

18-Feb-2025

Term 1/Week 3

Variables

- Introduction to (Week 2!)
Bapu Sesha-prasad!

- Computer Variable
- Variable $\left\{ \begin{array}{l} \text{Computer Variable} \\ \text{Algebraic Variable} \end{array} \right.$

- Computer variable is a 'pseudo' address for a memory location.

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- Hence, changes the value of address '9' to 33.
- Note that the expression $x = x + 1$ is valid in computers.
 $x = 15 + 1 = 16$
The value at address '1' is changed to 16.
- Hence '=' in computer essentially means 'access' and 'store' the value in physical address.

Physical Address

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Variable	Physical Address	Value	0	10
x	1	25	1	25
y	3	18	2	12
z	9	16	3	18
				⋮
			9	16

- Hence a computer variable is essentially convenient address specifier for the user.

$x = 15$ - changes the value from 25 to 15.

• $z = x + y = 15 + 18 = 33$

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- An Algebraic Variable (Latin "variabilis" or "changeable") is a symbol typically a letter that refers to an unspecified mathematical object.
 - Colloquially, a variable represents an object.
- For Ex. 4 apples $\Rightarrow 4a$
where 'a' represents 'apple'
- It can also be 4b!

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(European!)

In early modern period:

- Francis Viète (1540-1603)

introduced

Vowels \Rightarrow Variables

Consonants \Rightarrow Constants

Variable \Rightarrow unknown value

Constant \Rightarrow known value

- Rene Descartes (1596-1650)

introduced the convention of x, y & z for unknowns

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- Leonhard Euler (1707-1783)

introduced the concept of general 'function' of variables

Ex: $y = f(x)$

where $f(x) = x + 1$

- Carl Gauss (1777-1855)

introduced functions of 'complex' variables.

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in equations and a, b & c for knowns

- This is still in common use even today!

- Isaac Newton (1642-1727)
Gottfried Leibniz (1646-1716)

introduced 'calculus' which dealt with time varying variables namely $x(t)$ & rate of change
 \dot{x} - Newton
 dx/dt - Leibniz

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- Lastly, Variables, quadratic equations & cubic equations were used much before.

- Babylonians (1500 BC)

- Euclid (300 BC)

- Diophantus of Alexandria (200 AD)

- Brahmagupta (600 AD)
Complete treatise on mathematics!