

USA Maths

24-Feb-2026

Term 1 / week 5

Δt_{re} (Time elapsed at dist ' r_e ')
 $= 8.64 \times 10^4 \sqrt{1 - \frac{2 \times 6.67408 \times 10^{-11} \times 5.972 \times 10^{24}}{6.371 \times 10^6 \times (2.998)^2 \times 10^{16}}}$

Effects of Gravity

Homework (Calculator Precision)

Time dilation due to Earth's Gravity as per Einstein's General Relativity

$$= 8.64 \times 10^4 \sqrt{1 - \frac{79.715211520 \times 10^{13}}{57.262,573,484 \times 10^{22}}}$$

$$= 8.64 \times 10^4 \sqrt{1 - 1.392,099,703 \times 10^{-9}}$$

$$\Delta t_r = \Delta t_0 \sqrt{1 - \frac{2GM}{rc^2}}$$

$$= 8.64 \times 10^4 \sqrt{0.999,999,998,608}$$

$$= 86,399.999,939,866, \dots$$

Given $\Delta t_0 = 24 \text{ hrs } (8.6400 \times 10^4 \text{ s})$

$$G = 6.67408 \times 10^{-11}$$

$$M = 5.972 \times 10^{24} \text{ kg}$$

$$c = 2.998 \times 10^8 \text{ m/s}$$

Similarly,

$$\Delta t_{rs} = 86,399.999,985,471, \dots$$

(dist. to surface of earth) $r_e = 6.371 \times 10^6 \text{ m}$

(dist to satellite) $r_s = 26.371 \times 10^6 \text{ m}$

(Time elapsed at a distance ' r_s ' from the centre of earth)

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The calculator needs to have at least 10 to 12 digit precision

IEEE 754 Single Precision (1+8+23 bits)
 corresponds to 7 decimal digit precision

IEEE 754 Double Precision (1+11+52 bits)
 corresponds to 16 decimal digit precision

For International System of units (SI units)

$M_1, \& M_2 \Rightarrow \text{kg}$ (kilograms)

$r \Rightarrow \text{m}$ (meters)

Gravitational force

The Equation for gravitational force was developed by Newton

Newton's Law

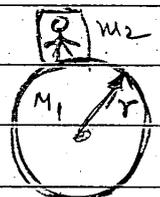
The force of attraction between two bodies with mass m_1 & m_2 at distance ' r ' is:

$$F_g = G \frac{m_1 m_2}{r^2}$$

$G \Rightarrow$ Gravitational Constant
 $= 6.67408 \times 10^{-11} \text{ N m}^2/\text{kg}^2$

Ex.1

Let us now analyse the effect of gravity on a person standing on earth



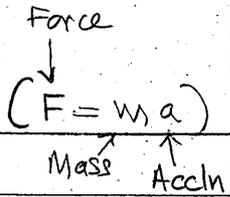
As per Newton's law:

$$F_g = G \frac{M_1 m_2}{r^2}$$

Also, we have that force acting on the person is the weight of the person!

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Say $F_g = m \cdot g$



where g - Accn due to gravity

For a person standing on Earth

$$F_g = F_g$$

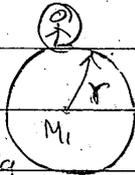
$$m \cdot g = G \cdot \frac{M_1 \cdot m_2}{r^2}$$

$$\therefore \text{Accn due to Gravity } (g) = \frac{G M_1}{r^2}$$

where $G = 6.67408 \times 10^{-11} \text{ N} \cdot \text{m}^2/\text{kg}^2$
 $M_1 = 5.972 \times 10^{24} \text{ kg}$ (Mass of Earth)
 $r = 6,371 \text{ km}$ ($6.371 \times 10^6 \text{ m}$)

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Note: 'G' is a universal constant, so, it remains the same.



Mass of Moon (M_1) = $7.35 \times 10^{22} \text{ kg}$
 Radius of Moon (r) = $1,737 \text{ km}$ ($1.737 \times 10^6 \text{ m}$)

$$\therefore g_m = \frac{G M_1}{r^2} = \frac{6.67408 \times 10^{-11} \times 7.35 \times 10^{22}}{(1.737 \times 10^6)^2}$$

$$= \frac{6.67408 \times 7.35 \times 10^{-11} \times 10^{22}}{(1.737)^2 \times 10^{12}}$$

$$= 16.258 \times 10^{-1}$$

$$= \underline{1.6258 \text{ m/s}^2}$$

Ex 3 Calculate the weight or force exerted by a person with a mass of 75 kg on the moon.

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$$\therefore g = \frac{6.67408 \times 10^{-11} \times 5.972 \times 10^{24}}{(6.371 \times 10^6)^2}$$

$$= \underline{9.81 \text{ m/s}^2}$$

\therefore Force exerted by a person

of 75 kg is

$$F_g = m \times g$$

$$= 75 \times 9.81 \text{ N} = \underline{735 \text{ N}}$$

Ex 2

Calculate the acceleration due to gravity on the moon.

We can use the same eqn as above with parameters of the moon.

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$$F_{g_m} = m \times g_m$$

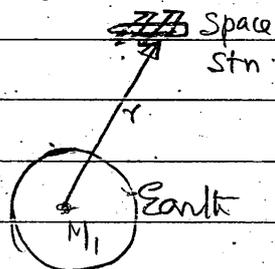
$$= 75 \times 1.6258 \text{ N} = \underline{122 \text{ N}}$$

The same person with a mass of 75 kg will be about 6 times lighter on the moon!

Ex 4

Calculate the acceleration due to earth's gravity on the space station for the given parameters.

(Earth) $M_1 = 5.972 \times 10^{24} \text{ kg}$
 dist. to Spacestn. $r = (6371 + 559) \text{ km}$
 $= 6.93 \times 10^6 \text{ m}$
 $G = 6.67408 \times 10^{-11}$



We can use the same Eqn as above

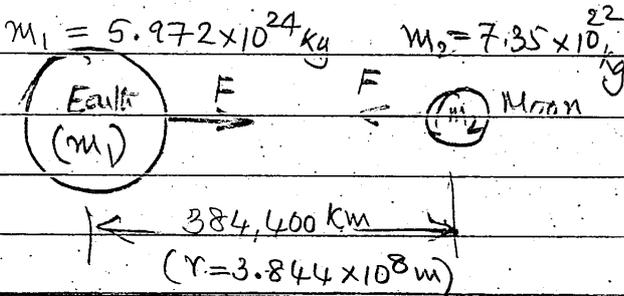
$$g = \frac{GM_1}{r^2} = \frac{6.67408 \times 10^{-11} \times 5.972 \times 10^{24}}{(6.93 \times 10^6)^2}$$

$$= 8.299 \text{ m/s}^2$$

[Substantial gravity! Weightlessness is due to free fall of space stn.]

Ex. 5

Calculate the force of attraction between the Earth and the moon



Home work

The mass of Jupiter is $1.9 \times 10^{27} \text{ kg}$ and its radius is 71,000 km.

- (a) Calculate the acceleration due to gravity on the surface of the Jupiter
- (b) What will be the weight of the person with a mass of 65 kg.

Ans.

- (a) 25.14 m/s²
- (b) 1,634 N

Using Newton's law

$$F = G \frac{m_1 m_2}{r^2}$$

$$= \frac{6.67408 \times 10^{-11} \times 5.972 \times 10^{24} \times 7.35 \times 10^{22}}{(3.844 \times 10^8)^2}$$

$$= 19.856 \times 10^9 \times 10^{16}$$

$$= 1.9856 \times 10^{20} \text{ N}$$